

Before 1000 BC

- ca. [70,000 BC](#) - [South Africa](#), ochre rocks adorned with scratched [geometric patterns](#)
- ca. [35,000 BC](#) to [20,000 BC](#) - [Africa](#) and [France](#), earliest known [prehistoric](#) attempts to quantify time
- ca. [20,000 BC](#) - [Nile Valley](#), [Ishango Bone](#): possibly the earliest reference to [prime numbers](#) and [Egyptian multiplication](#)
- ca. [3400 BC](#) - [Mesopotamia](#), the [Sumerians](#) invent the first [numeral system](#), and a system of [weights and measures](#)
- ca. [3100 BC](#) - [Egypt](#), earliest known [decimal system](#) allows indefinite counting by way of introducing new symbols, [\[5\]](#)
- ca. [2800 BC](#) - [Indus Valley Civilization](#) on the [Indian subcontinent](#), earliest use of [decimal ratios](#) in a uniform system of [ancient weights and measures](#), the smallest unit of measurement used is 1.704 millimetres and the smallest unit of mass used is 28 grams.
- [2800 BC](#) - The [Lo Shu Square](#), the unique normal [magic square](#) of order three, was discovered in [China](#).
- [2700 BC](#) - [Egypt](#), precision [surveying](#)
- [2600 BC](#) - [Indus Valley Civilization](#) - objects, streets, pavements, houses, and multi-storied buildings are constructed at perfect right angles, with each brick having the same dimensions
- [2400 BC](#) - [Egypt](#), precise [astronomical calendar](#), used even in the [Middle Ages](#) for its mathematical regularity
- ca. [2000 BC](#) - [Mesopotamia](#), the [Babylonians](#) use a base-60 decimal system, and compute the first known approximate value of π at 3.125
- [1800 BC](#) - [Moscow Mathematical Papyrus](#), findings volume of a frustum
- ca. [1800 BC](#) - [Vedic India](#) - [Yajnavalkya](#) writes the [Shatapatha Brahmana](#), in which he describes the motions of the sun and the moon, and advances a 95-year cycle to synchronize the motions of the sun and the moon
- ca. [1800 BC](#) - the [Yajur Veda](#), one of the four [Hindu Vedas](#), contains the earliest concept of [infinity](#), and states that "if you remove a part from infinity or add a part to infinity, still what remains is infinity"
- [1650 BC](#) - [Rhind Mathematical Papyrus](#), copy of a lost scroll from around 1850 BC, the scribe [Ahmes](#) presents one of the first known approximate values of π at 3.16, the first attempt at [squaring the circle](#), earliest known use of a sort of [cotangent](#), and knowledge of solving first order linear equations
- [1350 BC](#) - [Indian](#) astronomer [Lagadha](#) writes the "Vedanga Jyotisha", a [Vedic](#) text on [astronomy](#) that describes rules for tracking the motions of the sun and the moon, and uses [geometry](#) and [trigonometry](#) for astronomy
- [1300 BC](#) - [Berlin papyrus](#) (19th dynasty) contains a quadratic equation and its solution. [\[6\]](#)

1st millennium BC

- ca. [1000 BC](#) - [Vulgar fractions](#) used by the [Egyptians](#).

- [800 BC](#) - [Baudhayana](#), author of the Baudhayana [Sulba Sutra](#), a [Vedic Sanskrit](#) geometric text, contains the first use of the [Pythagorean theorem](#), [quadratic equations](#), and calculates the [square root](#) of 2 correct to five decimal places
- [600 BC](#) - [Apastamba](#), author of the Apastamba [Sulba Sutra](#), another [Vedic Sanskrit](#) geometric text, makes an attempt at [squaring the circle](#) and also calculates the [square root](#) of 2 correct to five decimal places
- ca. [600 BC](#) - the other [Vedic "Sulba Sutras"](#) ("rule of chords" in [Sanskrit](#)) use [Pythagorean triples](#), contain a number of geometrical proofs, and approximate π at 3.16
- [530 BC](#) - [Pythagoras](#) studies propositional [geometry](#) and vibrating lyre strings; his group also discover the [irrationality](#) of the [square root](#) of [two](#),
- ca. [500 BC](#) - [Indian](#) grammarian [Pānini](#), considered the father of [computing machines](#), writes the [Astadhyayi](#), which contains the use of metarules, [transformations](#) and [recursions](#), originally for the purpose of systematising the grammar of [Sanskrit](#)
- ca. [400 BC](#) - [Jaina](#) mathematicians in [India](#) write the "Surya Prajinapti", a mathematical text which classifies all numbers into three sets: enumerable, innumerable and [infinite](#). It also recognises five different types of [infinity](#): infinite in one and two directions, infinite in area, infinite everywhere, and infinite perpetually.
- [300s BC](#) - [Indian](#) texts use the [Sanskrit](#) word "Shunya" to refer to the concept of 'void' ([zero](#))
- [370 BC](#) - [Eudoxus](#) states the [method of exhaustion](#) for [area](#) determination,
- [350 BC](#) - [Aristotle](#) discusses [logical](#) reasoning in *Organon*,
- [300 BC](#) - [Jaina](#) mathematicians in [India](#) write the "Bhagabati Sutra", which contains the earliest information on [combinations](#)
- [300 BC](#) - [Euclid](#) in his *Elements* studies [geometry](#) as an [axiomatic system](#), proves the [infinitude](#) of [prime numbers](#) and presents the [Euclidean algorithm](#); he states the law of reflection in *Catoptrics*, and he proves the [fundamental theorem of arithmetic](#)
- ca. [300 BC](#) - [Brahmi numerals](#) are conceived in [India](#)
- [300 BC](#) - [Mesopotamia](#), the [Babylonians](#) invent the earliest calculator, the [abacus](#)
- ca. [300 BC](#) - [Indian mathematician Pingala](#) writes the "Chhandah-shastra", which contains the first Indian use of [zero](#) as a digit (indicated by a dot) and also presents a description of a [binary numeral system](#), along with the first use of [Fibonacci numbers](#) and [Pascal's triangle](#)
- [260 BC](#) - [Archimedes](#) develops a method to prove the value of π to within two decimal places using inscribed and circumscribed [polygons](#) and computes the area under a [parabolic segment](#),
- ca. [250 BC](#) - late [Olmecs](#) had already begun to use a true [zero](#) (a shell glyph) several centuries before [Ptolemy](#) in the New World. See [0 \(number\)](#).
- [240 BC](#) - [Eratosthenes](#) uses [his sieve algorithm](#) to quickly isolate [prime numbers](#),
- [225 BC](#) - [Apollonius of Perga](#) writes *On Conic Sections* and names the [ellipse](#), [parabola](#), and [hyperbola](#),
- [150 BC](#) - [Jain](#) mathematicians in [India](#) write the "Sthananga Sutra", which contains work on the theory of numbers, arithmetical operations, [geometry](#),

- operations with [fractions](#), simple equations, [cubic equations](#), quartic equations, and [permutations](#) and [combinations](#)
- [140 BC](#) - [Hipparchus](#) develops the bases of [trigonometry](#),
 - [50 BC](#) - [Indian numerals](#), the first [positional notation base-10 numeral system](#), begins developing in [India](#)

1st millennium

- [1st century](#) - [Heron of Alexandria](#), the earliest fleeting reference to square roots of negative numbers.
- ca. [200s](#) - [Ptolemy](#) of [Alexandria](#) wrote the [Almagest](#),
- [250](#) - [Diophantus](#) uses symbols for unknown numbers in terms of the [syncopated algebra](#), and he writes *Arithmetica*, the first systematic treatise on [algebra](#),
- [300](#) - the earliest known use of [zero](#) as a decimal digit is introduced by [Indian mathematicians](#)
- [400](#) - the "Bakhshali manuscript" is written by [Jaina](#) mathematicians, which describes a theory of the infinite containing different levels of [infinity](#), shows an understanding of [indices](#), as well as [logarithms](#) to [base 2](#), and computes [square roots](#) of numbers as large as a million correct to at least 11 decimal places
- [450](#) - [Zu Chongzhi](#) computes π to seven decimal places,
- [500](#) - [Aryabhata](#) writes the "Aryabhata-Siddhanta", which first introduces the trigonometric functions and methods of calculating their approximate numerical values. It defines the concepts of [sine](#) and [cosine](#), and also contains the earliest tables of sine and cosine values (in 3.75-degree intervals from 0 to 90 degrees)
- [500s](#) - [Aryabhata](#) gives accurate calculations for astronomical constants, such as the [solar eclipse](#) and [lunar eclipse](#), computes π to four decimal places, and obtains whole number solutions to [linear equations](#) by a method equivalent to the modern method
- [550](#) - [Hindu](#) mathematicians give [zero](#) a numeral representation in the [positional notation Indian numeral](#) system
- [600s](#) - [Bhaskara I](#) gives a rational approximation of the sine function
- [600s](#) - [Brahmagupta](#) invents the method of solving indeterminate equations of the second degree and is the first to use algebra to solve astronomical problems. He also develops methods for calculations of the motions and places of various planets, their rising and setting, conjunctions, and the calculation of eclipses of the sun and the moon
- [628](#) - [Brahmagupta](#) writes the *Brahma-sphuta-siddhanta*, where zero is clearly explained, and where the modern [place-value Indian numeral](#) system is fully developed. It also gives rules for manipulating both [negative and positive numbers](#), methods for computing [square roots](#), methods of solving [linear](#) and [quadratic equations](#), and rules for summing [series](#), [Brahmagupta's identity](#), and the [Brahmagupta theorem](#)
- [700s](#) - [Virasena](#) gives explicit rules for the [Fibonacci sequence](#), gives the derivation of the [volume](#) of a [frustum](#) using an [infinite](#) procedure, and also deals with the [logarithm](#) to [base 2](#) and knows its laws

- [700s](#) - [Shridhara](#) gives the rule for finding the volume of a sphere and also the formula for solving quadratic equations
- [750](#) - [Al-Khawarizmi](#) - Considered father of modern algebra since he was the first to bring Indian mathematics to Europe. First mathematician to work on the details of 'Arithmetic and Algebra of inheritance' besides the systematisation of the theory of linear and quadratic equations.
- [773](#) - Kanka brings [Brahmagupta's Brahma-sphuta-siddhanta](#) to [Baghdad](#) to explain the [Indian](#) system of arithmetic [astronomy](#) and the [Indian numeral](#) system
- [773](#) - Al Fazaii translates the [Brahma-sphuta-siddhanta](#) into [Arabic](#) upon the request of King Khalif Abbasid Al Mansoor
- [800s](#) - [Govindsvamin](#) discovers the Newton-Gauss interpolation formula, and gives the fractional parts of [Aryabhata's](#) tabular [sines](#)
- [895](#) - [Thabit ibn Qurra](#) - The only surviving fragment of his original work contains a chapter on the solution and properties of [cubic equations](#).
- [953](#) - [Al-Uqlidisi](#) writes the earliest translation on the Indian [place-value numeral system](#)
- [975](#) - [Al-Batani](#) - Extended the Indian concepts of sine and cosine to other trigonometrical ratios, like tangent, secant and their inverse functions. Derived the formula: $\sin \alpha = \tan \alpha / (1 + \tan^2 \alpha)$ and $\cos \alpha = 1 / (1 + \tan^2 \alpha)$.

1000 - 1499

- [1020](#) - [Abul Wáfa](#) - Gave this famous formula: $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \sin \beta \cos \alpha$. Also discussed the quadrature of the [parabola](#) and the volume of the [paraboloid](#).
- [1030](#) - [Ali Ahmad Nasawi](#) - Divides hours into 60 minutes and minutes into 60 seconds.
- [1070](#) - [Omar Khayyám](#) begins to write *Treatise on Demonstration of Problems of Algebra* and classifies cubic equations.
- [1100s](#) - [Indian numerals](#) have been modified by [Arab](#) mathematicians to form the modern [Hindu-Arabic numeral](#) system (used universally in the modern world)
- [1100s](#) - the [Hindu-Arabic numeral](#) system reaches [Europe](#) through the [Arabs](#)
- [1100s](#) - [Bhaskara Acharya](#) writes the [Lilavati](#), which covers the topics of definitions, arithmetical terms, interest computation, arithmetical and geometrical progressions, [plane geometry](#), [solid geometry](#), the shadow of the [gnomon](#), methods to solve indeterminate equations, and [combinations](#)
- [1100s](#) - [Bhaskara Acharya](#) writes the "Bijaganita" ("[Algebra](#)"), which is the first text to recognize that a positive number has two square roots
- [1100s](#) - [Bhaskara Acharya](#) conceives [differential calculus](#), and also develops [Rolle's theorem](#), [Pell's equation](#), a proof for the [Pythagorean Theorem](#), proves that division by zero is infinity, computes π to 5 decimal places, and calculates the time taken for the earth to orbit the sun to 9 decimal places
- [1202](#) - [Leonardo Fibonacci](#) demonstrates the utility of [Hindu-Arabic numerals](#) in his *Book of the Abacus*,
- [1303](#) - [Zhu Shijie](#) publishes *Precious Mirror of the Four Elements*, which contains an ancient method of arranging [binomial coefficients](#) in a triangle.

- [1300s](#) - [Madhava](#) is considered the father of [mathematical analysis](#), who also worked on the power series for p and for sine and cosine functions, and along with other [Kerala school](#) mathematicians, founded the important concepts of [Calculus](#)
- [1300s](#) - [Parameshvara](#), a [Kerala school](#) mathematician, presents a series form of the [sine function](#) that is equivalent to its [Taylor series](#) expansion, states the [mean value theorem](#) of [differential calculus](#), and is also the first mathematician to give the radius of circle with inscribed [cyclic quadrilateral](#)
- [1400](#) - [Madhava](#) discovers the series expansion for the inverse-tangent function, the infinite series for arctan and sin, and many methods for calculating the circumference of the circle, and uses them to compute π correct to 11 decimal places
- [1424](#) - [Ghiyath al-Kashi](#) - computes π to sixteen decimal places using inscribed and circumscribed polygons,
- [1400s](#) - [Nilakantha Somayaji](#), a [Kerala school](#) mathematician, writes the "Aryabhatiya Bhasya", which contains work on infinite-series expansions, problems of algebra, and spherical geometry
- [1478](#) - An anonymous author writes the [Treviso Arithmetic](#).

16th century

- [1501](#) - [Nilakantha Somayaji](#) writes the "Tantra Samgraha", which lays the foundation for a complete system of fluxions ([derivatives](#)), and expands on concepts from his previous text, the "Aryabhatiya Bhasya"
- [1520](#) - [Scipione dal Ferro](#) develops a method for solving "depressed" cubic equations (cubic equations without an x^2 term), but does not publish,
- [1535](#) - [Niccolo Tartaglia](#) independently develops a method for solving depressed cubic equations but also does not publish,
- [1539](#) - [Gerolamo Cardano](#) learns Tartaglia's method for solving depressed cubics and discovers a method for depressing cubics, thereby creating a method for solving all cubics,
- [1540](#) - [Lodovico Ferrari](#) solves the [quartic equation](#),
- [1544](#) - [Michael Stifel](#) publishes "Arithmetica integra",
- [1550](#) - [Jyeshtadeva](#), a [Kerala school](#) mathematician, writes the "Yuktibhasa", the world's first [calculus](#) text, which gives detailed derivations of many calculus theorems and formulae
- [1596](#) - Ludolf van Ceulen computes π to twenty decimal places using inscribed and circumscribed polygons,

17th century

- [1600s](#) - Putumana Somayaji writes the "Paddhati", which presents a detailed discussion of various trigonometric series
- [1614](#) - [John Napier](#) discusses Napierian [logarithms](#) in *Mirifici Logarithmorum Canonis Descriptio*,

- [1617](#) - [Henry Briggs](#) discusses decimal logarithms in *Logarithmorum Chilias Prima*,
- [1618](#) - [John Napier](#) publishes the first references to e in a work on [logarithms](#).
- [1619](#) - [René Descartes](#) discovers [analytic geometry](#) ([Pierre de Fermat](#) claimed that he also discovered it independently),
- [1619](#) - [Johannes Kepler](#) discovers two of the [Kepler-Poinsot polyhedra](#).
- [1629](#) - [Pierre de Fermat](#) develops a rudimentary [differential calculus](#),
- [1634](#) - [Gilles de Roberval](#) shows that the area under a [cycloid](#) is three times the area of its generating circle,
- [1637](#) - [Pierre de Fermat](#) claims to have proven [Fermat's last theorem](#) in his copy of Diophantus' *Arithmetica*,
- [1637](#) - First use of the term [imaginary number](#) by [René Descartes](#), it was meant to be derogatory.
- [1654](#) - [Blaise Pascal](#) and [Pierre de Fermat](#) create the theory of [probability](#),
- [1655](#) - [John Wallis](#) writes *Arithmetica Infinitorum*,
- [1658](#) - [Christopher Wren](#) shows that the length of a [cycloid](#) is four times the diameter of its generating circle,
- [1665](#) - [Isaac Newton](#) works on the [fundamental theorem of calculus](#) and develops his version of [infinitesimal calculus](#),
- [1668](#) - [Nicholas Mercator](#) and [William Brouncker](#) discover an [infinite series](#) for the logarithm while attempting to calculate the area under a [hyperbolic segment](#),
- [1671](#) - [James Gregory](#) develops a series expansion for the inverse-[tangent](#) function (originally discovered by [Madhava](#))
- [1673](#) - [Gottfried Leibniz](#) also develops his version of [infinitesimal calculus](#),
- [1675](#) - [Isaac Newton](#) invents an algorithm for the [computation of functional roots](#),
- [1680s](#) - [Gottfried Leibniz](#) works on symbolic logic,
- [1691](#) - [Gottfried Leibniz](#) discovers the technique of separation of variables for ordinary [differential equations](#),
- [1693](#) - [Edmund Halley](#) prepares the first mortality tables statistically relating death rate to age,
- [1696](#) - [Guillaume de L'Hôpital](#) states [his rule](#) for the computation of certain [limits](#),
- [1696](#) - [Jakob Bernoulli](#) and [Johann Bernoulli](#) solve [brachistochrone problem](#), the first result in the [calculus of variations](#),

18th century

- [1706](#) - [John Machin](#) develops a quickly converging inverse-tangent series for π and computes π to 100 decimal places,
- [1712](#) - [Brook Taylor](#) develops [Taylor series](#),
- [1722](#) - [Abraham De Moivre](#) states [De Moivre's theorem](#) connecting [trigonometric functions](#) and [complex numbers](#),
- [1724](#) - [Abraham De Moivre](#) studies mortality statistics and the foundation of the theory of annuities in *Annuities on Lives*,
- [1730](#) - [James Stirling](#) publishes *The Differential Method*,
- [1733](#) - [Giovanni Gerolamo Saccheri](#) studies what geometry would be like if [Euclid's fifth postulate](#) were false,

- 1733 - [Abraham de Moivre](#) introduces the [normal distribution](#) to approximate the [binomial distribution](#) in probability,
- 1734 - [Leonhard Euler](#) introduces the [integrating factor technique](#) for solving first-order ordinary [differential equations](#),
- 1735 - [Leonhard Euler](#) solves the [Basel problem](#), relating an infinite series to π ,
- 1736 - [Leonhard Euler](#) solves the problem of the [Seven bridges of Königsberg](#), in effect creating [graph theory](#),
- 1739 - [Leonhard Euler](#) solves the general [homogeneous linear ordinary differential equation](#) with [constant coefficients](#),
- 1742 - [Christian Goldbach](#) conjectures that every even number greater than two can be expressed as the sum of two primes, now known as [Goldbach's conjecture](#),
- 1748 - [Maria Gaetana Agnesi](#) discusses analysis in *Instituzioni Analitiche ad Uso della Gioventu Italiana*,
- 1761 - [Thomas Bayes](#) proves [Bayes' theorem](#),
- 1762 - [Joseph Louis Lagrange](#) discovers the [divergence theorem](#),
- 1789 - [Jurij Vega](#) improves Machin's formula and computes π to 140 decimal places,
- 1794 - [Jurij Vega](#) publishes *Thesaurus Logarithmorum Completus*,
- 1796 - [Carl Friedrich Gauss](#) proves that the [regular 17-gon](#) can be constructed using only a [compass and straightedge](#)
- 1796 - [Adrien-Marie Legendre](#) conjectures the [prime number theorem](#),
- 1797 - [Caspar Wessel](#) associates vectors with [complex numbers](#) and studies complex number operations in geometrical terms,
- 1799 - [Carl Friedrich Gauss](#) proves the [fundamental theorem of algebra](#) (every polynomial equation has a solution among the complex numbers),
- 1799 - [Paolo Ruffini](#) partially proves the [Abel–Ruffini theorem](#) that [quintic](#) or higher equations cannot be solved by a general formula,

19th century

- 1801 - *Disquisitiones Arithmeticae*, [Carl Friedrich Gauss's number theory](#) treatise, is published in Latin
- 1805 - [Adrien-Marie Legendre](#) introduces the [method of least squares](#) for fitting a curve to a given set of observations,
- 1806 - [Louis Poinsot](#) discovers the two remaining [Kepler-Poinsot polyhedra](#).
- 1807 - [Joseph Fourier](#) announces his discoveries about the [trigonometric decomposition of functions](#),
- 1811 - [Carl Friedrich Gauss](#) discusses the meaning of integrals with complex limits and briefly examines the dependence of such integrals on the chosen path of integration,
- 1815 - [Siméon-Denis Poisson](#) carries out integrations along paths in the complex plane,
- 1817 - [Bernard Bolzano](#) presents the [intermediate value theorem](#)---a [continuous function](#) which is negative at one point and positive at another point must be zero for at least one point in between,

- [1822](#) - [Augustin-Louis Cauchy](#) presents the [Cauchy integral theorem](#) for integration around the boundary of a rectangle in the [complex plane](#),
- [1824](#) - [Niels Henrik Abel](#) partially proves the [Abel–Ruffini theorem](#) that the general [quintic](#) or higher equations cannot be solved by a general formula involving only arithmetical operations and roots,
- [1825](#) - Augustin-Louis Cauchy presents the [Cauchy integral theorem](#) for general integration paths -- he assumes the function being integrated has a continuous derivative, and he introduces the theory of [residues](#) in [complex analysis](#),
- [1825](#) - [Johann Peter Gustav Lejeune Dirichlet](#) and Adrien-Marie Legendre prove Fermat's last theorem for $n = 5$,
- [1825](#) - [André-Marie Ampère](#) discovers [Stokes' theorem](#),
- [1828](#) - George Green proves [Green's theorem](#),
- [1829](#) - [Nikolai Ivanovich Lobachevsky](#) publishes his work on hyperbolic [non-Euclidean geometry](#),
- [1831](#) - [Mikhail Vasilievich Ostrogradsky](#) rediscovers and gives the first proof of the divergence theorem earlier described by Lagrange, Gauss and Green,
- [1832](#) - [Évariste Galois](#) presents a general condition for the solvability of [algebraic equations](#), thereby essentially founding [group theory](#) and [Galois theory](#),
- [1832](#) - Peter Dirichlet proves Fermat's last theorem for $n = 14$,
- [1835](#) - Peter Dirichlet proves [Dirichlet's theorem](#) about prime numbers in arithmetical progressions,
- [1837](#) - [Pierre Wantzel](#) proves that doubling the cube and trisecting the angle are impossible with only a compass and straightedge, as well as the full completion of the problem of constructability of regular polygons
- [1841](#) - [Karl Weierstrass](#) discovers but does not publish the [Laurent expansion theorem](#),
- [1843](#) - [Pierre-Alphonse Laurent](#) discovers and presents the Laurent expansion theorem,
- [1843](#) - [William Hamilton](#) discovers the calculus of [quaternions](#) and deduces that they are non-commutative,
- [1847](#) - [George Boole](#) formalizes [symbolic logic](#) in *The Mathematical Analysis of Logic*, defining what are now called [Boolean algebras](#),
- [1849](#) - [George Gabriel Stokes](#) shows that [solitary waves](#) can arise from a combination of periodic waves,
- [1850](#) - [Victor Alexandre Puiseux](#) distinguishes between poles and branch points and introduces the concept of [essential singular points](#),
- [1850](#) - George Gabriel Stokes rediscovers and proves [Stokes' theorem](#),
- [1854](#) - [Bernhard Riemann](#) introduces [Riemannian geometry](#),
- [1854](#) - [Arthur Cayley](#) shows that [quaternions](#) can be used to represent rotations in four-dimensional [space](#),
- [1858](#) - [August Ferdinand Möbius](#) invents the [Möbius strip](#),
- [1859](#) - Bernhard Riemann formulates the [Riemann hypothesis](#) which has strong implications about the distribution of [prime numbers](#),
- [1870](#) - [Felix Klein](#) constructs an analytic geometry for Lobachevski's geometry thereby establishing its self-consistency and the logical independence of Euclid's fifth postulate,

- [1873](#) - [Charles Hermite](#) proves that e is transcendental,
- [1873](#) - [Georg Frobenius](#) presents his method for finding series solutions to linear differential equations with [regular singular points](#),
- [1874](#) - [Georg Cantor](#) shows that the set of all [real numbers](#) is [uncountably infinite](#) but the set of all [algebraic numbers](#) is [countably infinite](#). Contrary to widely held beliefs, his method was not his famous [diagonal argument](#), which he published three years later. (Nor did he formulate [set theory](#) at this time.)
- [1878](#) - Charles Hermite solves the general quintic equation by means of elliptic and modular functions
- [1882](#) - [Ferdinand von Lindemann](#) proves that π is transcendental and that therefore the circle cannot be squared with a compass and straightedge,
- [1882](#) - Felix Klein invents the [Klein bottle](#),
- [1895](#) - [Diederik Korteweg](#) and [Gustav de Vries](#) derive the [KdV equation](#) to describe the development of long solitary water waves in a canal of rectangular cross section,
- [1895](#) - [Georg Cantor](#) publishes a book about set theory containing the arithmetic of infinite [cardinal numbers](#) and the [continuum hypothesis](#),
- [1896](#) - [Jacques Hadamard](#) and [Charles Jean de la Vallée-Poussin](#) independently prove the [prime number theorem](#),
- [1896](#) - [Hermann Minkowski](#) presents *Geometry of numbers*,
- [1899](#) - [Georg Cantor](#) discovers a contradiction in his set theory,
- [1899](#) - [David Hilbert](#) presents a set of self-consistent geometric axioms in *Foundations of Geometry*,

20th century

- [1900](#) - David Hilbert states his [list of 23 problems](#) which show where some further mathematical work is needed,
- [1901](#) - [Élie Cartan](#) develops the [exterior derivative](#),
- [1903](#) - [Carle David Tolme Runge](#) presents a [fast Fourier Transform](#) algorithm,
- [1903](#) - [Edmund Georg Hermann Landau](#) gives considerably simpler proof of the prime number theorem,
- [1908](#) - [Ernst Zermelo](#) axiomizes [set theory](#), thus avoiding Cantor's contradictions,
- [1908](#) - [Josip Plemelj](#) solves the Riemann problem about the existence of a differential equation with a given [monodromic group](#) and uses Sokhotsky - Plemelj formulae,
- [1912](#) - [Luitzen Egbertus Jan Brouwer](#) presents the [Brouwer fixed-point theorem](#),
- [1912](#) - Josip Plemelj publishes simplified proof for the Fermat's last theorem for exponent $n = 5$,
- [1913](#) - [Srinivasa Aaiyengar Ramanujan](#) sends a long list of complex theorems without proofs to [G. H. Hardy](#),
- [1914](#) - [Srinivasa Aaiyengar Ramanujan](#) publishes *Modular Equations and Approximations to π* ,
- [1910s](#) - [Srinivasa Aaiyengar Ramanujan](#) develops over 3000 theorems, including properties of [highly composite numbers](#), the [partition function](#) and its [asymptotics](#), and [mock theta functions](#). He also makes major breakthroughs and

- discoveries in the areas of [gamma functions](#), [modular forms](#), [divergent series](#), [hypergeometric series](#) and [prime number theory](#)
- 1919 - [Viggo Brun](#) defines [Brun's constant](#) B_2 for [twin primes](#),
 - 1928 - [John von Neumann](#) begins devising the principles of [game theory](#) and proves the [minimax theorem](#),
 - 1930 - [Casimir Kuratowski](#) shows that the [three cottage problem](#) has no solution,
 - 1931 - [Kurt Gödel](#) proves [his incompleteness theorem](#) which shows that every axiomatic system for mathematics is either incomplete or inconsistent,
 - 1931 - [Georges de Rham](#) develops theorems in [cohomology](#) and [characteristic classes](#),
 - 1933 - [Karol Borsuk](#) and [Stanislaw Ulam](#) present the [Borsuk-Ulam antipodal-point theorem](#),
 - 1933 - [Andrey Nikolaevich Kolmogorov](#) publishes his book *Basic notions of the calculus of probability* (*Grundbegriffe der Wahrscheinlichkeitsrechnung*) which contains an [axiomatization of probability](#) based on [measure theory](#),
 - 1940 - Kurt Gödel shows that neither the [continuum hypothesis](#) nor the [axiom of choice](#) can be disproven from the standard axioms of set theory,
 - 1942 - [G.C. Danielson](#) and [Cornelius Lanczos](#) develop a [Fast Fourier Transform](#) algorithm,
 - 1943 - [Kenneth Levenberg](#) proposes a method for nonlinear least squares fitting,
 - 1948 - John von Neumann mathematically studies self-reproducing machines,
 - 1949 - John von Neumann computes π to 2,037 decimal places using [ENIAC](#),
 - 1950 - Stanislaw Ulam and John von Neumann present [cellular automata](#) dynamical systems,
 - 1953 - [Nicholas Metropolis](#) introduces the idea of thermodynamic [simulated annealing](#) algorithms,
 - 1955 - [H. S. M. Coxeter](#) et al. publish the complete list of [uniform polyhedron](#),
 - 1955 - [Enrico Fermi](#), [John Pasta](#), and Stanislaw Ulam numerically study a nonlinear spring model of heat conduction and discover solitary wave type behavior,
 - 1960 - [C. A. R. Hoare](#) invents the [quicksort](#) algorithm,
 - 1960 - [Irving S. Reed](#) and [Gustave Solomon](#) present the [Reed-Solomon error-correcting code](#),
 - 1961 - [Daniel Shanks](#) and [John Wrench](#) compute π to 100,000 decimal places using an inverse-tangent identity and an IBM-7090 computer,
 - 1962 - [Donald Marquardt](#) proposes the [Levenberg-Marquardt nonlinear least squares fitting algorithm](#),
 - 1963 - [Paul Cohen](#) uses his technique of [forcing](#) to show that neither the [continuum hypothesis](#) nor the [axiom of choice](#) can be proven from the standard axioms of set theory,
 - 1963 - [Martin Kruskal](#) and [Norman Zabusky](#) analytically study the [Fermi-Pasta-Ulam heat conduction problem](#) in the continuum limit and find that the [KdV equation](#) governs this system,
 - 1963 - meteorologist and mathematician [Edward Norton Lorenz](#) published solutions for a simplified mathematical model of atmospheric turbulence -

- generally known as chaotic behaviour and [strange attractors](#) or [Lorenz Attractor](#) - also the [Butterfly Effect](#)
- [1965](#) - Martin Kruskal and Norman Zabusky numerically study colliding [solitary waves](#) in [plasmas](#) and find that they do not disperse after collisions,
 - [1965](#) - [James Cooley](#) and [John Tukey](#) present an influential [Fast Fourier Transform](#) algorithm,
 - [1966](#) - [E.J. Putzer](#) presents two methods for computing the [exponential of a matrix](#) in terms of a polynomial in that matrix,
 - [1966](#) - [Abraham Robinson](#) presents [Non-standard analysis](#).
 - [1967](#) - [Robert Langlands](#) formulates the influential [Langlands program](#) of conjectures relating number theory and representation theory,
 - [1968](#) - [Michael Atiyah](#) and [Isadore Singer](#) prove the [Atiyah-Singer index theorem](#) about the index of [elliptic operators](#),
 - [1975](#) - [Benoît Mandelbrot](#) published *Les objets fractals, forme, hasard et dimension*,
 - [1976](#) - [Kenneth Appel](#) and [Wolfgang Haken](#) use a computer to prove the [Four color theorem](#),
 - [1983](#) - [Gerd Faltings](#) proves the [Mordell conjecture](#) and thereby shows that there are only finitely many whole number solutions for each exponent of Fermat's last theorem,
 - [1983](#) - the [classification of finite simple groups](#), a collaborative work involving some hundred mathematicians and spanning thirty years, is completed,
 - [1985](#) - [Louis de Branges de Bourcia](#) proves the [Bieberbach conjecture](#),
 - [1987](#) - [Yasumasa Kanada](#), [David Bailey](#), [Jonathan Borwein](#), and [Peter Borwein](#) use iterative modular equation approximations to elliptic integrals and a [NEC SX-2 supercomputer](#) to compute π to 134 million decimal places,
 - [1991](#) - [Alain Connes](#) and [John W. Lott](#) develop [non-commutative geometry](#),
 - [1994](#) - [Andrew Wiles](#) proves part of the [Taniyama-Shimura conjecture](#) and thereby proves Fermat's last theorem,
 - [1998](#) - [Thomas Hales](#) (almost certainly) proves the [Kepler conjecture](#),
 - [1999](#) - the full [Taniyama-Shimura conjecture](#) is proved.

21st century

- [2000](#) - the [Clay Mathematics Institute](#) establishes the seven Millennium Prize Problems of unsolved important classic mathematical questions,
- [2002](#) - [Manindra Agrawal](#), [Nitin Saxena](#), and [Neeraj Kayal](#) of [IIT Kanpur](#) present an unconditional deterministic [polynomial time](#) algorithm to determine whether a given number is [prime](#),
- [2002](#) - [Yasumasa Kanada](#), Y. Ushiro, [Hisayasu Kuroda](#), [Makoto Kudoh](#) and a team of nine more compute π to 1241.1 billion digits using a [Hitachi](#) 64-node [supercomputer](#),
- [2002](#) - [Preda Mihăilescu](#) proves [Catalan's conjecture](#),
- [2003](#) - [Grigori Perelman](#) proves the [Poincaré conjecture](#),
- [2007](#) - a team of researchers throughout North America and Europe used networks of computers to map [E8 \(mathematics\)](#).^[1]

